

AN APPROACH FOR DETERMINING THE BEST SOLUTION FOR INTUITIONISTIC FUZZY TRANSPORTATION PROBLEM

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Abstract: The research study determines the best optimal solution to a usual kind of optimization issue which is known as problem of intuitionistic fuzzy transportation using triangular fuzzy values. The triangular values in terms of fuzzy shows the utility of the worth or the prices, supply, requirement, request, order and demand for solving the problems of transportation in terms of fuzzy values. The major motive of this study is to obtain the lowest entire transportation worth of commodities which fulfils the requirements of the consumers from different origins to the different landing places. For this, an approach named Vogel's Approximation Method is implementing for getting desired answer.

Keywords: *Transportation Problem, Tri-angular fuzzy values, Vogel's-Approximation-Method (VAM).*

Introduction

The compliance of transportation has been considered as a type of linear-programming. In this problem, commodities are shifted from m origins to n landing places having dimensions $u_1, u_2, u_3, \dots, u_m$ and $v_1, v_2, v_3, \dots, v_n$. Moreover, c_{ij} shows a cost associated with penalties of goods which are to be shifted from different origins i.e. i to different landing places i.e. j . These penalties are considered as cost, price, flexibility in delivery, time of delivery, security of delivery of goods, etc. The unspecified commodity which is to be shifted from m origins to n landing places is denoted by x_{ij} . A compliance concerning fuzzy-transportation is that where transportation amounts concerning prices, requirement, request, order as well as command are considered in terms of fuzzy values.

The major motive of this paper is the computation of the shipped scheme for fuzzy-transportation compliance for obtaining the lowest entire worth of fuzzy-transportation by considering that the limited part of order and requirement through tri-angular intuitionistic-fuzzy values is applying to compute the best optimize answers for the fuzzy-transportation compliance. The major interest of intuitionistic-fuzzy theory marks the gradation of the membership & non-membership function of every member for fuzzy sets and also easily deals with the concept of uncertainty when compared with fuzzy sets. Thus, this study is an effort to answer the problem of the

intuitionistic fuzzy transportation by transporting goods or commodities from different origins to different landing places by considering lowest costs and highest gains by tri-angular intuitionistic-fuzzy numerals through VAM approach.

Literature Review

Firstly, the fundamental framework of developing the difficulty related to transportation had been introduced by Hitchcock [1] integrated with the problems of LPP. The major motive of the transportation compliance is to shipped goods or commodities from different origins to different landing places by considering lowest costs and highest gains. The three approaches termed as north-west-corner rule, least-cost entry rule and VAM are commonly implemented to calculate the answer initially for transportation compliance. Among all these approaches, VAM approach is precise and accurate to determine the best and appropriate optimal solution of a transportation problem and also shows better results when compared to the entire method of the transportation problem [2,19].

A fuzzy concept was discovered by Zadeh [3]. Chanas and Kuchta [4] introduced the conceptualization of the best optimize answer of the fuzzy transportation compliance through the application of the fuzzy values as well as presented a procedure for attaining the required optimal answer. Atanassov in [5] suggested the concept of sets having properties' of Intuitionistic Fuzzy and named as IFSs which are applicable to overcome the problem of uncertainty. Many researchers have answered the problem related to intuitionistic fuzzy transportation in which they transform the supplies and demand accessibilities from fuzzy to crisp numerals (Hussain & Kumar [6]; Nagoorgani & Abbas [7]).

Antony et al. [8] answered the problem of transportation by using intuitionistic fuzzy values through VAM approach and find the best optimize final answer. But the drawback is that they did not show the details of optimality factor for finding the best optimal answer. Singh & Yadav [9] applied an excellent algorithm to answer the type-one problem of the intuitionistic fuzzy transportation. Ebrahimnejad and Verdegay [10] introduced an excellent mathematical technique to solve the problems of type-II intuitionistic fuzzy transportation through the application of fuzzy numerals. Singh & Yadav [11] developed an approach to answer the problems of intuitionistic fuzzy-transportation through the application of fuzzy values. Annie Christi [12] answered the problems of intuitionistic fuzzy transportation through the application of pentagonal fuzzy numerals by using the ranking method and Russell's technique.

Bharati & Malhotra [13] introduced an approach to solve the problem of transportation in two-stage through the application of the intuitionistic fuzzy values. Gupta & Anjum [14] implemented a new technique to solve the problem of transportation of type-II by using intuitionistic fuzzy values. Roy et al. [15] applied an efficient method to answer the multiple-objective problems of intuitionistic-fuzzy-transportation through the application of fuzzy values. Mahmoodirad et al. [16] applied an approach to answer the difficulties of completely

intuitionistic fuzzy transportation through the application of fuzzy terms. Kumar [17] implemented a new extended technique based on intuitionistic fuzzy zero point to solve the problems of type-II intuitionistic-fuzzy-transportation through the application of fuzzy numerals. Karagul & Sahin [20] presented a novel approximation method to obtain initial basic feasible solution of transportation problem. Chhibber et al. [21] analysed a problem from fuzzy transportation problem to non-linear intuitionistic fuzzy multi-objective transportation problem. Ahmed et al. [22] applied a fuzzy multi-objective defuzzification method to solve a transportation problem. Zhu et al. [23] applied a fixed charge transportation problem with damageable items under uncertain environment.

The structure of this paper is: Preliminaries are shown in part three where as in part four, procedures of the VAM approach are discussed. In part fifth, numerical part of 4x4 Intuitionistic-Fuzzy-Transportation-Problem is estimated. The outcomes as well as future upcoming was shown in part 6.

Preliminaries -Definition 3.1 Fuzzy Set –Suppose U is a non-blank group. A fuzzy set F of U is stated as: $F = \{ \langle x, \mu_F(x) \rangle \mid x \in U \}$. Here, $\mu_F(x)$ is termed as membership function lies between zero and one.

Definition 3.2 Fuzzy Number –It does not consider only one value but considers a group of attainable values which lies between zero and one.

Definition 3.3 Tri-angular Fuzzy Numeral -A Tri-angular fuzzy numeral F is designated as 3 sub-strings (m_1, m_2, m_3) which show that $m_1 \leq m_2 \leq m_3$ with membership function is as under:

$$\mu_F(x) = \frac{x - m_1}{m_2 - m_1} ; \text{ for } m_1 \leq x \leq m_2$$

$$\frac{m_3 - x}{m_3 - m_2} ; \text{ for } m_2 \leq x \leq m_3$$

zero ; otherwise

Definition 3.4 Intuitionistic Tri-angular Fuzzy Numeral-A Intuitionistic Tri-angular fuzzy numeral F^I is denoted by $F^I = (m_1, m_2, m_3)(m'_1, m'_2, m'_3)$ where $m'_1 \leq m_1 \leq m_2 \leq m_3 \leq m'_3$ with membership $\mu_{F^I}(x)$ and non-membership function $v_{F^I}(x)$.

$$\mu_{F^I}(x) = \frac{x - m_1}{m_2 - m_1} ; \text{ for } m_1 \leq x \leq m_2$$

$$\frac{m_3 - x}{m_3 - m_2} ; \text{ for } m_2 \leq x \leq m_3$$

zero ; otherwise

$$v_F^l(x) = \frac{m_2 - x}{m_2 - m_1'} ; \text{ for } m_1' \leq x \leq m_2$$

$$\frac{x - m_2}{m_3' - m_2} ; \text{ for } m_2 \leq x \leq m_3'$$

1 ; otherwise

Definition 3.5 Arithmetic processes of tri-angular fuzzy numerals- Let I and J be two positive triangular fuzzy numbers. Hence, the main algebraic operations are: $I = (l, m, n)$ and $J = (u, v, w)$ (Wu et al. 2009 [18]) is:

- (i) Addition (+) : $I + J = (l, m, n) + (u, v, w) = (l + u, m + v, n + w)$
- (ii) Subtraction (-) : $I - J = (l, m, n) - (u, v, w) = (l - u, m - v, n - w)$
- (iii) Multiplication(\times) : $I \times J = (l, m, n) \times (u, v, w) = (l \times u, m \times v, n \times w)$
- (iv) Division (\div) : $I \div J = (l, m, n) \div (u, v, w) = \left(\frac{l}{u}, \frac{m}{v}, \frac{n}{w}\right)$

Methodology

Step 1- Examine that the whole order is same as whole requirement. Step 2- Computing the best and optimize answer through VAM approach. For finding penalties of all rows/columns by taking the differences of the two cells which has the minimum cost in that row/column. Step 3- Select greatest cost of penalty. Step 4- Allocate that cell having least cost of transportation and greatest cost of penalty in rows / columns. Step 5-Estimate an optimize answer of the intuitionistic-fuzzy-transportation compliance. Step 6- Compute the entire min. cost of

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods
O ₁	16	1	8	13	<(2,4,5)(1,4,6)>
O ₂	11	4	7	10	<(4,6,8)(3,6,9)>
O ₃	8	15	9	2	<(3,7,12)(2,7,13)>
O ₄	6	12	5	14	<(8,10,13)(5,10,16)>
Demand	<(3,4,6)(1,4,8)>	<(2,5,7)(1,5,8)>	<(10,15,20)(8,15,22)>	<(2,3,5)(1,3,6)>	

the goods.

Numerical Analysis

Table1 4×4 Intuitionistic-Fuzzy-Transportation-Problem (IFTP)

Solution- In this problem, supply is same as demand by using step 1. Through step 2, computing the penalties of all the rows/columns which depicts Table 2. Through step 3, selecting the highest penalty at col. 4 i.e. 8. Allocate the max. attainable components to min. cost location at (3,4) i.e. $\langle(2,3,5)(1,3,6)\rangle$. Showing the rest in row 3 by eliminating the 4th col. by dotted line) that depicts Table 2. Repeat steps 2, 3 & 4.

Table 2 Showing penalties and allocation in cell (3,4)

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods	Penalties
O ₁	16	1	8	13	$\langle(2,4,5)(1,4,6)\rangle$	7
O ₂	11	4	7	10	$\langle(4,6,8)(3,6,9)\rangle$	3
O ₃	8	15	9	2[$\langle(2,3,5)(1,3,6)\rangle$]	$\langle(3,7,12)(2,7,13)\rangle/\langle(-2,4,10)(-4,4,12)\rangle$	1
O ₄	6	12	5	14	$\langle(8,10,13)(5,10,16)\rangle$	1
Demand	$\langle(3,4,6)(1,4,8)\rangle$	$\langle(2,5,7)(1,5,8)\rangle$	$\langle(10,15,20)(8,15,22)\rangle$	$\langle(2,3,5)(1,3,6)\rangle$		
Penalties	2	3	2	8		

Repeating step 3, selecting the highest penalty in row 1 i.e. 7. Allocating the max. attainable components to the min. cost location at (1,2) i.e. $\langle(2,4,5)(1,4,6)\rangle$. Showing the rest in row 2, by eliminating the 1st row by dotted line that depicts Table 3.

Table 3 Showing penalties and allocation in cell (1,2)

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods	Penalty
O ₁	16	1[$\langle(2,4,5)(1,4,6)\rangle$]	8		$\langle(2,4,5)(1,4,6)\rangle$	7
O ₂	11	4	7		$\langle(4,6,8)(3,6,9)\rangle$	3
O ₃	8	15	9	2[$\langle(2,3,5)(1,3,6)\rangle$]	$\langle(-2,4,10)(-4,4,12)\rangle$	1
O ₄	6	12	5		$\langle(8,10,13)(5,10,16)\rangle$	1
Demand	$\langle(3,4,6)(1,4,8)\rangle$	$\langle(2,5,7)(1,5,8)\rangle/\langle(3,1,5)(-5,1,7)\rangle$	$\langle(10,15,20)(8,15,22)\rangle$			
Penalty	2	3	2			

Repeating step 3, selecting the highest penalty at col. 2 i.e. 8. Allocating the max. attainable components to the min. cost location at (2,2) i.e. $\langle(-3,1,5)(-5,1,7)\rangle$. Showing the rest in row 2, after eliminating the 2ndcol. by dotted line that depicts Table 4.

Table 4 Showing penalties and allocation in cell (2,2)

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods	Penalty
O ₁	16	1 $\langle(2,4,5)(1,4,6)\rangle$	8		$\langle(2,4,5)(1,4,6)\rangle$	7
O ₂	11	4 $\langle(-3,1,5)(-5,1,7)\rangle$	7		$\langle(4,6,8)(3,6,9)\rangle$	3
O ₃	8	15	9	2 $\langle(2,3,5)(1,3,6)\rangle$	$\langle(-2,4,10)(-4,4,12)\rangle$	1
O ₄	6	12	5		$\langle(8,10,13)(5,10,16)\rangle$	1
Demand	$\langle(3,4,6)(1,4,8)\rangle$	$\langle(-3,1,5)(-5,1,7)\rangle/0$	$\langle(10,15,20)(8,15,22)\rangle$			
Penalty	2	8 \updownarrow	2			

Repeating step 3, selecting the highest penalty at row 2 i.e. 4. Now allocate the max. attainable components to the min. cost location at (2,3) i.e. $\langle(-1,5,11)(-4,5,14)\rangle$. Showing the rest in row 2, by eliminating the 2nd row by dotted line that depicts Table 5.

Table 5 Showing penalties and allocation in cell (2,3)

Repeating step 3, selecting the highest penalty at row 3 i.e. 8. Allocating the max. attainable components to the min. cost location at

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods	Penalty
O ₁		1 $\langle(2,4,5)(1,4,6)\rangle$				
O ₂		4 $\langle(-3,1,5)(-5,1,7)\rangle$	7 $\langle(-1,5,11)(-4,5,14)\rangle$			4 \leftrightarrow
O ₃	8		9	2 $\langle(2,3,5)(1,3,6)\rangle$	$\langle(-2,4,10)(-4,4,12)\rangle$	1
O ₄	6		5		$\langle(8,10,13)(5,10,16)\rangle$	1
Demand	$\langle(3,4,6)(1,4,8)\rangle$		$\langle(10,15,20)(8,15,22)\rangle/\langle(-1,10,21)(-6,10,26)\rangle$			
Penalty	2		4			

(3,1) i.e. $\langle(-2,4,10)(-4,4,12)\rangle$. Showing the rest in row 3, after eliminating the 3rd row by dotted line that depicts Table 6.

Table 6 Showing penalties and allocation in cell (3,1)

Repeating step 3, selecting the highest penalty at row 4 i.e. 6. Now allocate the max. attainable components to

Order/Demand	D ₁	D ₂	D ₃	D ₄	Goods	Penalty
O ₁		1[<(2,4,5)(1,4,6)>]				
O ₂		4[<(-3,1,5)(-5,1,7)>]	7[<(-1,5,11)(-4,5,14)>]			
O ₃	8[<(-2,4,10)(-4,4,12)>]			2[<(2,3,5)(1,3,6)>]	<(-2,4,10)(-4,4,12)>/0	8 ↔
O ₄	6		5[<(-1,10,21)(-6,10,26)>]		<(-13,0,14)(-21,0,22)>	6
Demand	<(3,4,6)(1,4,8)>/<(-7,0,8)(-11,0,12)>					
Penalty	2					

the min. cost location at (4,1) i.e.<(-7,0,8)(-11,0,12)>. Showing the rest in row 4, after eliminating the 1st column by dotted line that depicts Table 7.

Table 7 Showing penalties and allocation in cell (4,1)

Order/Demand	D ₁	D ₂	D ₃	D ₄	IF Goods	Penalty
O ₁		1[<(2,4,5)(1,4,6)>]				
O ₂		4[<(-3,1,5)(-5,1,7)>]	7[<(-1,5,11)(-4,5,14)>]			
O ₃	8[<(-2,4,10)(-4,4,12)>]			2[<(2,3,5)(1,3,6)>]		
O ₄	6[<(-7,0,8)(-11,0,12)>]		5[<(-1,10,21)(-6,10,26)>]		<(-13,0,14)(-21,0,22)>	6 ↔
Demand	<(-7,0,8)(-11,0,12)>					

	11,0,12)>/0					
Penalty	6					

The intuitionistic fuzzy optimal answer through is as under:

$$X_{12} = (2,4,5)(1,4,6), X_{22} = (-3,1,5)(-5,1,7), X_{23} = (-1,5,11)(-4,5,14), X_{31} = (-2,4,10)(-4,4,12), X_{34} = (2,3,5)(1,3,6),$$

$$X_{41} = (-7,0,8)(-11,0,12), X_{43} = (-1,10,21)(-6,10,26).$$

Thus, the min. cost is: $Min. z = 1 \times (2,4,5)(1,4,6) + 4 \times (-3,1,5)(-5,1,7) + 7 \times (-1,5,11)(-4,5,14) + 8 \times (-2,4,10)(-4,4,12) + 2 \times (2,3,5)(1,3,6) + 6 \times (-7,0,8)(-11,0,12) + 5 \times (-1,10,21)(-6,10,26) = (2,4,5)(1,4,6) + (-12,4,20)(-20,4,28) + (-7,35,77)(-28,35,98) + (-16,32,80)(-32,32,96) + (4,6,10)(2,6,12) + (-42,0,48)(-66,0,72) + (-5,50,105)(-30,50,130) = (-76,131,345)(-173,131,442).$

Discussion

By using fuzzy transportation, we optimize the solution of the demand and supply. During the solving of the intuitionistic fuzzy numbers, we face the problem to minimize the cost of the transportation to reduce the transportation cost by taking the penalty method. We reduce the transportation cost and obtain the optimization the minimum transportation cost in a more effective way. By this research, we got the advantage to reduce the logistic cost by optimal solution. But the limitation of using this method is that it is little bit more computational process as in every table we have to find the penalty level. As future considerations, this method is more effective for all types of industries to optimize the transportation cost.

Conclusion

In this study, we compute the best optimize answer by answering the compliance of fuzzy-transportation by VAM method through tri-angular fuzzy numerals. The algorithmic steps observed in the study are relevant when the supplies, costs, penalties, requirements, orders and demands exist in real numerals and IFNs. In future study, we are going to upgrade the algorithmic steps for answering the difficulty issue of transportation with supplies, costs, penalties, requirements, orders, etc. It also modified to answer the issue in transportation when the supplies, costs, penalties, requirements, orders, etc. are of various kinds.

References

[1] Hitchcock, F. L. (1941). The distribution of a product from several sources to numerous localities. *Journal of mathematics and physics*, 20(1-4), 224-230.

[2]Reinfeld, N.V., Vogel, W.R. (1958): *Mathematical Programming*, Prentice-Hall, Englewood Cliftspp. 59–70.

[3] Zadeh, L. A. (1965). Fuzzy sets. *Information and control*, 8(3), 338-353.

- [4] Chanas, S., &Kuchta, D. (1996). A concept of the optimal solution of the transportation problem with fuzzy cost coefficients. *Fuzzy sets and systems*, 82(3), 299-305.
- [5] Atanassov .K.T. (1986) “Intuitionistic Fuzzy Sets”, *Fuzzy sets and systems*, Vol.20 (1), pp: 87-9
- [6] Hussain, R. J., & Kumar, P. S. (2012). Algorithmic approach for solving intuitionistic fuzzy transportation problem. *Applied mathematical sciences*, 6(80), 3981-3989.
- [7] Gani, A. N., & Abbas, S. (2013). A new method for solving intuitionistic fuzzy transportation problem. *Applied Mathematical Sciences*, 7(28), 1357-1365.
- [8] Antony, R. J. P., Savarimuthu, S. J., &Pathinathan, T. (2014). Method for solving the transportation problem using triangular intuitionistic fuzzy number. *International Journal of Computing Algorithm*, 3(1), 590-605.
- [9] Singh, S. K., &Yadav, S. P. (2015). Efficient approach for solving type-1 intuitionistic fuzzy transportation problem. *International journal of system assurance engineering and management*, 6, 259-267.
- [9] Antony, R. J. P., Savarimuthu, S. J., &Pathinathan, T. (2014). Method for solving the transportation problem using triangular intuitionistic fuzzy number. *International Journal of Computing Algorithm*, 3(1), 590-605.
- [10] Ebrahimnejad, A., &Verdegay, J. L. (2016). An efficient computational approach for solving type-2 intuitionistic fuzzy numbers based transportation problems. *International Journal of Computational Intelligence Systems*, 9(6), 1154-1173.
- [11] Singh, S. K., &Yadav, S. P. (2016). A novel approach for solving fully intuitionistic fuzzy transportation problem. *International journal of operational research*, 26(4), 460-472.
- [12] Christi, M. A., &Kasthuri, B. (2016).Transportation Problem with Pentagonal Intuitionistic Fuzzy Numbers Solved Using Ranking Technique and Russell’s Method; *Int. Journal of Engineering Research and Applications*, 6(2), 82-86.
- [13] Bharati, S. K., &Malhotra, R. (2017). Two stage intuitionistic fuzzy time minimizing transportation problem based on generalized Zadeh’s extension principle. *International Journal of System Assurance Engineering and Management*, 8, 1442-1449.
- [14] Gupta, G., &Anupum, K. (2017). An efficient method for solving intuitionistic fuzzy transportation problem of type-2. *International Journal of Applied and Computational Mathematics*, 3, 3795-3804.
- [15]Roy, S. K., Ebrahimnejad, A., Verdegay, J. L., & Das, S. (2018). New approach for solving intuitionistic fuzzy multi-objective transportation problem. *Sādhanā*, 43, 1-12.
- [16] Mahmoodirad, A., Allahviranloo, T., &Niroomand, S. (2019). A new effective solution method for fully intuitionistic fuzzy transportation problem. *Soft computing*, 23(12), 4521-4530.
- [17] Kumar, P. S. (2020). Intuitionistic fuzzy zero point method for solving type-2 intuitionistic fuzzy transportation problem. *International journal of operational research*, 37(3), 418-451.
- [18] Wu, H. Y.; Tzeng, G. H.; Chen, Y. H. 2009. A fuzzy MCDM approach for evaluating banking performance based on balanced scorecard, *Expert Systems with Applications* 36: 10135–10147.
- [19] Agarwal, R., Agrawal, A., Kumar, N., Shah, M. A., Jawla, P., Priyan, S.,

"Benchmarking the Interactions among Green and Sustainable Vendor Selection Attributes", *Advances in Operations Research*, vol. 2022, Article ID 8966856, 11 pages, 2022. <https://doi.org/10.1155/2022/8966856>

[20] Karagul K and Sahin Y 2020 A novel Approximation method to obtain initial basic feasible solution of transportation problem. *Journal of King Saud University –Engineering Sciences* 33, pg 211-218.

[21] Chhibber, D.; Srivastava, P.K.; Bisht, D.C. From fuzzy transportation problem to non-linear intuitionistic fuzzy multi-objective transportation problem: A literature review. *Int. J. Model. Simul.* 2021, 41, 335–350.

[22] Ahmed, J.S.; Mohammed, H.J.; Chalob, I.Z. Application of a fuzzy multi-objective defuzzification method to solve a transportation problem. *Mater. Today Proc.* 2021.

[23] Zhu, K.; Ji, K.; Shen, J. A fixed charge transportation problem with damageable items under uncertain environment. *Phys. A: Stat. Mech. Its Appl.* 2021, 581, 126234.